Subject: Maths

Topic: Iteration

Topic/Skill	Definition/Tips	Example
1. Iteration	The act of repeating a process over and over again, often with the aim of approximating a desired result more closely. Recursive Notation: $x_{n+1} = \sqrt{3x_n + 6}$	$x_{1} = 4$ $x_{2} = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_{3} = \sqrt{3 \times 4.242640} \dots + 6$ $= 4.357576 \dots$
2. Iterative Method	 To create an iterative formula, rearrange an equation with more than one x term to make one of the x terms the subject. You will be given the first value to substitute in, often called x₁. Keep substituting in your previous answer until your answers are the same to a certain degree of accuracy. This is called converging to a limit. Use the 'ANS' button on your calculator to keep substituting in the previous answer. 	Use an iterative formula to find the positive root of $x^2 - 3x - 6 = 0$ to 3 decimal places. $x_1 = 4$ Answer: $x^2 = 3x + 6$ $x = \sqrt{3x} + 6$ So $x_{n+1} = \sqrt{3x_n + 6}$ $x_1 = 4$ $x_2 = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_3 = \sqrt{3 \times 4.242640} \dots + 6$ $= 4.357576 \dots$ Keep repeating $x_7 = 4.372068 \dots = 4.372 (3dp)$ $x_8 = 4.372208 \dots = 4.372 (3dp)$ So answer is $x = 4.372 (3dp)$